

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Write and solve each of the following linear equations.

a. Ofelia has a certain amount of money. If she spends \$12, then she has  $\frac{1}{5}$  of the original amount left. How much money did Ofelia have originally?

b. Three consecutive integers have a sum of 234. What are the three integers?

c. Gil is reading a book that has 276 pages. He already read some of it last week. He plans to read 20 pages tomorrow. By then, he will be  $\frac{2}{3}$  of the way through the book. How many pages did Gil read last week?

2. a. Without solving, identify whether each of the following equations has a unique solution, no solution, or infinitely many solutions.

i.  $3x + 5 = -2$

ii.  $6(x - 11) = 15 - 4x$

iii.  $12x + 9 = 8x + 1 + 4x$

iv.  $2(x - 3) = 10x - 6 - 8x$

v.  $5x + 6 = 5x - 4$

- b. Solve the following equation for a number  $x$ . Verify that your solution is correct.

$$-15 = 8x + 1$$

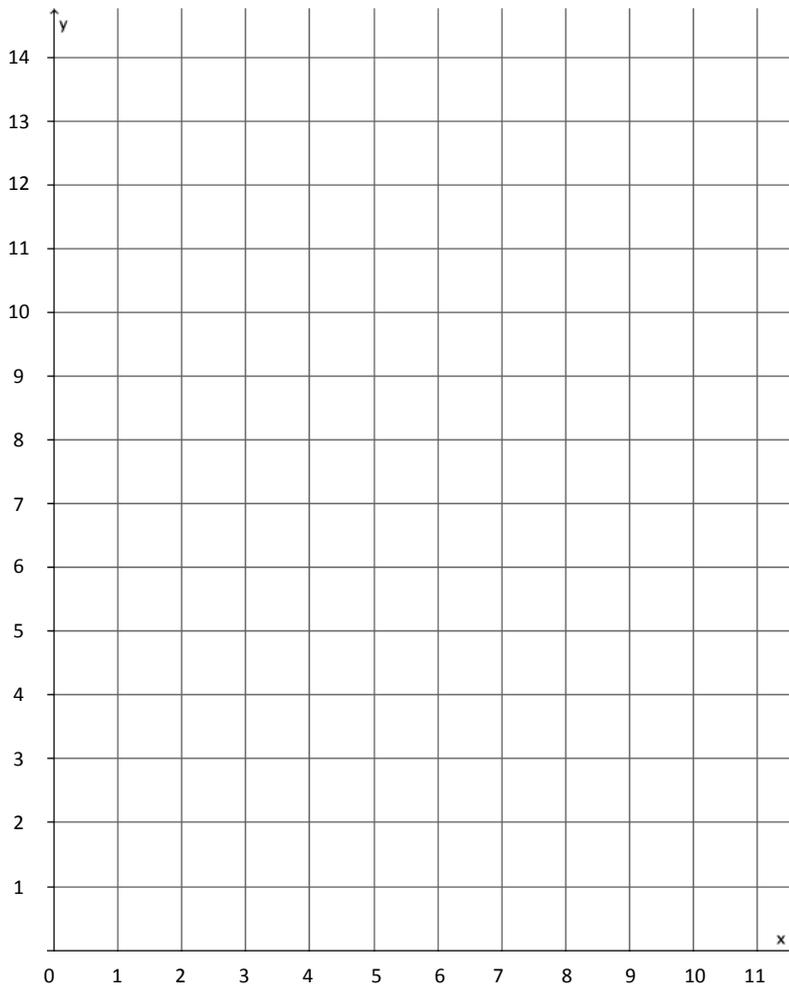
- c. Solve the following equation for a number  $x$ . Verify that your solution is correct.

$$7(2x + 5) = 4x - 9 - x$$

3. a. Parker paid \$4.50 for three pounds of gummy candy. Assuming each pound of gummy candy costs the same amount, complete the table of values representing the cost of gummy candy in pounds.

|                               |   |   |        |   |   |   |   |   |   |
|-------------------------------|---|---|--------|---|---|---|---|---|---|
| Gummy Candy in Pounds ( $x$ ) | 1 | 2 | 3      | 4 | 5 | 6 | 7 | 8 | 9 |
| Cost ( $y$ )                  |   |   | \$4.50 |   |   |   |   |   |   |

- b. Graph the data on the coordinate plane.



- c. On the same day, Parker's friend, Peggy, was charged \$5 for  $1\frac{1}{2}$  lb. of gummy candy. Explain in terms of the graph why this must be a mistake.

A Progression Toward Mastery

| Assessment Task Item |                       | STEP 1<br>Missing or incorrect answer and little evidence of reasoning or application of mathematics to solve the problem.                      | STEP 2<br>Missing or incorrect answer but evidence of some reasoning or application of mathematics to solve the problem.  | STEP 3<br>A correct answer with some evidence of reasoning or application of mathematics to solve the problem, <u>or</u> an incorrect answer with substantial evidence of solid reasoning or application of mathematics to solve the problem.  | STEP 4<br>A correct answer supported by substantial evidence of solid reasoning or application of mathematics to solve the problem.  |
|----------------------|-----------------------|---|---|--|--|
| 1                    | a<br><b>8.EE.C.7b</b> | Student makes no attempt to solve the problem or leaves the problem blank.<br><u>OR</u><br>Student may or may not have identified the variable. | Student does not set up an equation (i.e., guesses the answer).<br><u>OR</u><br>Student may or may not have identified the variable.  | Student may or may not have set up correct equation.<br><u>OR</u><br>Student may or may not have identified the variable.<br><u>OR</u><br>Student makes calculation errors.  | Student identifies the variable as, "Let $x$ be the amount of money Ofelia had," or something similar.<br><u>AND</u><br>Student sets up a correct equation, $x - 12 = \frac{1}{5}x$ , or other equivalent version.<br><u>AND</u><br>Student solves for the variable correctly, $x = 15$ .        |
|                      | b<br><b>8.EE.C.7b</b> | Student makes no attempt to solve the problem or leaves the problem blank.<br><u>OR</u><br>Student may or may not have identified the variable. | Student does not set up an equation (i.e., guesses the answer).<br><u>OR</u><br>Student may or may not have identified the variable.<br><u>OR</u><br>Student makes calculation errors.<br><u>OR</u><br>Student only answers part of the question, stating, for example, that the first number is 77, but does not give all three numbers. | Student attempts to set up an equation, but may have set up an incorrect equation.<br><u>OR</u><br>Student may or may not have identified the variable.<br><u>OR</u><br>Student makes calculation errors.<br><u>OR</u><br>Student only answers part of the question, stating, for example, that the first number is 77, but does not give all three numbers. | Student identifies the variable as, "Let $x$ be the first integer."<br><u>AND</u><br>Student sets up a correct equation, $3x + 3 = 234$ , or other equivalent version.<br><u>AND</u><br>Student solves the equation correctly and identifies all three numbers correctly (i.e., 77, 78, and 79). |

|          |                              |   |  |   |  |
|----------|------------------------------|---|--|---|--|
|          | <b>c</b><br><b>8.EE.C.7b</b> | Student makes no attempt to solve the problem or leaves the problem blank.<br><u>OR</u><br>Student may or may not have identified the variable.   | Student does not set up an equation (i.e., guesses the answer).<br><u>OR</u><br>Student may or may not have identified the variable.   | Student attempts to set up an equation, but may have set up an incorrect equation.<br><u>OR</u><br>Student may or may not have identified the variable.<br><u>OR</u><br>Student makes calculation errors leading to an incorrect answer.  | Student identifies the variable as, "Let $x$ be the number of pages Gil read last week," or something similar.<br><u>AND</u><br>Student sets up a correct equation, $x + 20 = 184$ , or other equivalent version.<br><u>AND</u><br>Student solves for the number of pages Gil read last week as 164 pages. |
| <b>2</b> | <b>a</b><br><b>8.EE.C.7a</b> | Student makes no attempt to determine the type of solution or leaves the problem blank.<br><u>OR</u><br>Student determines 0 of the solution types correctly.<br><u>OR</u><br>Student may have attempted to determine the solutions by solving. | Student determines 1–2 of the solution types correctly.<br><u>OR</u><br>Student may have attempted to determine the solutions by solving.  | Student determines 3–5 of the solution types correctly.<br><u>OR</u><br>Student may have attempted to determine the solutions by solving.   | Student determines 5 of the solutions types correctly. Equations 1 and 2 have unique solutions, equation 3 has no solution, equation 4 has infinitely many solutions, and equation 5 has no solution.<br><u>AND</u><br>Student determines the solutions by observation only.                               |
|          | <b>b</b><br><b>8.EE.C.7b</b> | Student makes no attempt to solve the problem or leaves the problem blank.  | Student uses properties of equality incorrectly, e.g., subtracts 1 from just one side of the equation, or divides by 8 on just one side of the equation, leading to an incorrect solution. | Student correctly uses properties of rational numbers to solve the equation but makes a computational error leading to an incorrect solution. For example, student may have subtracted 1 from each side of the equation, but $-15 - 1$ led to an incorrect answer. Student may or may not have verified the answer. | Student correctly uses properties of rational numbers to solve the equation (i.e., finds $x = -2$ ). There is evidence that the student verifies the solution.   |
|          | <b>c</b><br><b>8.EE.C.7b</b> | Student makes no attempt to solve the problem or leaves the problem blank.  | Student uses the distributive property incorrectly on both sides of the equation, e.g., $7(2x + 5) = 14x + 5$ or $4x - x = 4$ , leading to an incorrect solution.                          | Student uses the distributive property correctly on one or both sides of the equation, but makes a computational error leading to an incorrect solution. Student may or may not have verified the answer.   | Student uses the distributive property correctly on both sides of the equation leading to a correct solution (i.e., $x = -4$ ). There is evidence that the student verifies the solution.  |

|                               |  |   |   |  |   |                               |         |         |         |   |   |   |   |   |   |              |        |        |        |        |        |        |         |         |
|-------------------------------|--|---|---|--|---|-------------------------------|---------|---------|---------|---|---|---|---|---|---|--------------|--------|--------|--------|--------|--------|--------|---------|---------|
| <b>3</b>                      | <b>a</b><br><br><b>8.EE.B.5</b>  | Student makes no attempt to complete the table or uses completely random numbers in the blanks. | Student completes the table incorrectly but only because of a simple computational error in finding the cost of one pound of candy, leading to all other parts being incorrect. | Student completes 6–7 parts of the table correctly. A computational error leads to 1–2 parts being incorrect.  | Student completes all 8 parts of the table correctly. (See table below for correct answers.)  |                               |         |         |         |   |   |   |   |   |   |              |        |        |        |        |        |        |         |         |
|                               | <table border="1"> <tr> <td style="text-align: center;">Gummy Candy in Pounds (<math>x</math>)</td> <td style="text-align: center;">1</td> <td style="text-align: center;">2</td> <td style="text-align: center;">3</td> <td style="text-align: center;">4</td> <td style="text-align: center;">5</td> <td style="text-align: center;">6</td> <td style="text-align: center;">7</td> <td style="text-align: center;">8</td> <td style="text-align: center;">9</td> </tr> <tr> <td style="text-align: center;">Cost (<math>y</math>)</td> <td style="text-align: center;">\$1.50</td> <td style="text-align: center;">\$3.00</td> <td style="text-align: center;">\$4.50</td> <td style="text-align: center;">\$6.00</td> <td style="text-align: center;">\$7.50</td> <td style="text-align: center;">\$9.00</td> <td style="text-align: center;">\$10.50</td> <td style="text-align: center;">\$12.00</td> <td style="text-align: center;">\$13.50</td> </tr> </table> |   |   |  |   | Gummy Candy in Pounds ( $x$ ) | 1       | 2       | 3       | 4 | 5 | 6 | 7 | 8 | 9 | Cost ( $y$ ) | \$1.50 | \$3.00 | \$4.50 | \$6.00 | \$7.50 | \$9.00 | \$10.50 | \$12.00 |
| Gummy Candy in Pounds ( $x$ ) | 1  | 2   | 3   | 4  | 5   | 6                             | 7       | 8       | 9       |   |   |   |   |   |   |              |        |        |        |        |        |        |         |         |
| Cost ( $y$ )                  | \$1.50   | \$3.00  | \$4.50  | \$6.00   | \$7.50  | \$9.00                        | \$10.50 | \$12.00 | \$13.50 |   |   |   |   |   |   |              |        |        |        |        |        |        |         |         |
|                               | <b>b</b><br><br><b>8.EE.B.5</b>  | Student makes no attempt to put the data on the graph, or points are graphed randomly.          | Student plots data points on the graph but misplaces a few points.<br><u>OR</u><br>Student inverts the data (i.e., plots points according to $(y, x)$ instead of $(x, y)$ ).    | Student plots 6–7 data points correctly according to the data in the table.  | Student plots all 8 data points correctly according to the data in the table.   |                               |         |         |         |   |   |   |   |   |   |              |        |        |        |        |        |        |         |         |
|                               | <b>c</b><br><br><b>8.EE.B.5</b>  | Student leaves the problem blank.   | Student performs a computation to prove the mistake. Little or no reference to the graph is made in the argument.   | Student makes a weak argument as to why $(1.5, 5)$ could not be correct. Student may have connected the dots on the graph to show $(1.5, 5)$ could not be correct. | Student makes a convincing argument as to why the point $(1.5, 5)$ could not be correct. Student references the relationship being proportional and/or predicts that all points should fall into a line based on the existing pattern of points on the graph. |                               |         |         |         |   |   |   |   |   |   |              |        |        |        |        |        |        |         |         |

Name \_\_\_\_\_

Date \_\_\_\_\_

1. Write and solve each of the following linear equations.

- a. Ofelia has a certain amount of money. If she spends \$12, then she has  $\frac{1}{5}$  of the original amount left. How much money did Ofelia have originally?

LET  $x$  BE THE AMOUNT OF MONEY OFELIA HAD

$$\begin{aligned} x - 12 &= \frac{1}{5}x \\ x - \frac{1}{5}x - 12 + 12 &= \frac{1}{5}x - \frac{1}{5}x + 12 \\ \frac{4}{5}x &= 12 \\ x &= 12 \cdot \frac{5}{4} = \frac{60}{4} \end{aligned}$$

OFELIA HAD \$15.00 ORIGINALLY.

- b. Three consecutive integers have a sum of 234. What are the three integers?

LET  $x$  BE THE FIRST INTEGER

$$\begin{aligned} x + x + 1 + x + 2 &= 234 \\ 3x + 3 &= 234 \\ 3x + 3 - 3 &= 234 - 3 \\ 3x &= 231 \\ x &= 77 \end{aligned}$$

THE INTEGERS ARE 77, 78, AND 79.

- c. Gil is reading a book that has 276 pages. He already read some of it last week. He plans to read 20 pages tomorrow. By then, he will be  $\frac{2}{3}$  of the way through the book. How many pages did Gil read last week?

LET  $x$  BE THE NUMBER OF PAGES GIL READ LAST WEEK.

$$\begin{aligned} x + 20 &= \frac{2}{3}(276) \\ x + 20 &= 184 \\ x + 20 - 20 &= 184 - 20 \\ x &= 164 \end{aligned}$$

GIL READ 164 PAGES LAST WEEK.

2. a. Without solving, identify whether each of the following equations has a unique solution, no solution, or infinitely many solutions.

i.  $3x + 5 = -2$

UNIQUE

ii.  $6(x - 11) = 15 - 4x$

UNIQUE

iii.  $12x + 9 = 8x + 1 + 4x$

NO SOLUTION

iv.  $2(x - 3) = 10x - 6 - 8x$

INFINITELY MANY SOLUTIONS

v.  $5x + 6 = 5x - 4$

NO SOLUTION

b. Solve the following equation for a number  $x$ . Verify that your solution is correct.

$$\begin{array}{r} -15 = 8x + 1 \\ -1 \quad -1 \\ \hline -16 = 8x \\ \frac{-16}{8} = \frac{8x}{8} \\ -2 = x \end{array}$$

$$\begin{array}{l} -15 = 8(-2) + 1 \\ -15 = -16 + 1 \\ -15 = -15 \end{array}$$

c. Solve the following equation for a number  $x$ . Verify that your solution is correct.

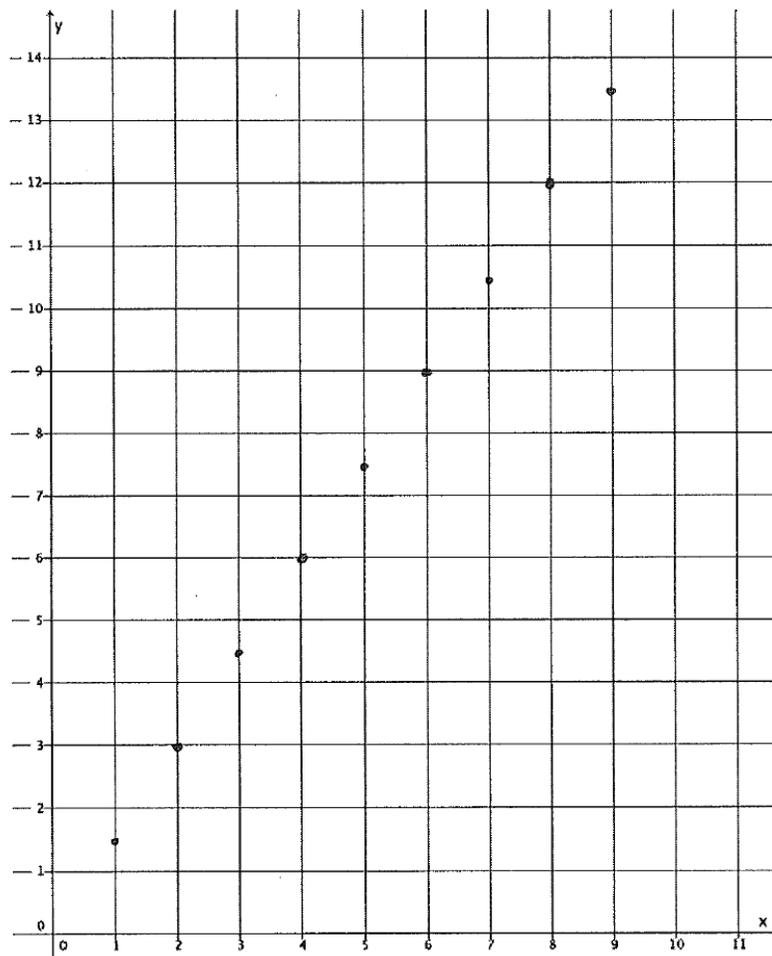
$$\begin{array}{l} 7(2x + 5) = 4x - 9 - x \\ 14x + 35 = 4x - x - 9 \\ 14x + 35 = 3x - 9 \\ 14x - 3x + 35 = 3x - 3x - 9 \\ 11x + 35 = -9 \\ 11x + 35 - 35 = -9 - 35 \\ 11x = -44 \\ x = -4 \end{array}$$

$$\begin{array}{l} 7(2(-4) + 5) = 4(-4) - 9 - (-4) \\ 7(-8 + 5) = -16 - 9 + 4 \\ 7(-3) = -25 + 4 \\ -21 = -21 \end{array}$$

3. a. Parker paid \$4.50 for three pounds of gummy candy. Assuming each pound of gummy candy costs the same amount, complete the table of values representing the cost of gummy candy in pounds.

| Gummy Candy in pounds ( $x$ ) | 1      | 2      | 3      | 4      | 5      | 6      | 7       | 8       | 9       |
|-------------------------------|--------|--------|--------|--------|--------|--------|---------|---------|---------|
| Cost ( $y$ )                  | \$1.50 | \$3.00 | \$4.50 | \$6.00 | \$7.50 | \$9.00 | \$10.50 | \$12.00 | \$13.50 |

- b. Graph the data on the coordinate plane.



- c. On the same day, Parker's friend, Peggy, was charged \$5 for  $1\frac{1}{2}$  lb. of gummy candy. Explain in terms of the graph why this must be a mistake.

EVEN THOUGH  $1\frac{1}{2}$  POUNDS OF CANDY ISN'T A POINT ON THE GRAPH, IT IS REASONABLE TO BELIEVE IT WILL FALL IN LINE WITH THE OTHER POINTS. THE COST OF  $1\frac{1}{2}$  POUNDS OF CANDY DOES NOT FIT THE PATTERN.